## **Functional Analysis 1**

## Course Syllabus

## Spring Term 2021 - SNU

Course Title Functional Analysis 1 (in English)

Course number 3341.603

Instructor Gerald Trutnau

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Course homepage http://www.math.snu.ac.kr/~trutnau/teachingFA12021.html

**Course Objective** We will study the main basic theorems and principles of functional analysis together with corresponding applications, in particular we cover: metric spaces, semi-norms, completeness, Banach and Hilbert spaces, function spaces, Sobolev spaces, separability, Stone-Weierstrass theorems, partition of unity, compactness, Arzela-Ascoli theorem, linear operators, Neumann series, Distributions, Linear functionals, Hahn-Banach theorems, Lax-Milgram theorem, dual space, weak convergence, reflexivity, Baire category theorem, Banach-Steinhaus theorem, open mapping theorem, closed graph theorem, projections, orthogonality.

**References** Here are some recommended references:

- Alt, Hans Wilhelm: Lineare Funktionalanalysis, Springer (unfortunately in German); 5th edition (2006), available as ebook at the central library

- Brézis, Haïm: Analyse fonctionnelle, Dunod (2002), and its new expanded English Edition: Functional Analysis, Sobolev Spaces and Partial Differential Equations, Springer; (2010)

- Lax, Peter D.: Functional Analysis, Wiley-Interscience (2002)

- Rudin, Walter: Functional Analysis, McGraw-Hill, 2 edition (1991)

- Yoshida, Kôsaku: Functional Analysis (Springer Classics in Mathematics) (6th edition, 1980)

**Evaluation** - Attendance: (will not be checked). However, students are supposed to know the material taught in class.

- Take Home Exam I (7-9th week, 40 % of final score);

- Take Home Exam II (13-15th week, 40 % of final score);

- Other: (20 % of final score, for instance additional homework in case a TA is assigned, etc. ... This will be discussed at the beginning of the course)