

COMPLEX SYMMETRY OF TRUNCATED SHIFT TYPE OPERATOR MATRIX AND ITS TRANSFORMS

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ABSTRACT. In this paper we study characterizations of a complex symmetric operator matrix. In particular, we consider operator transforms of a truncated shift type operator matrix. As some applications of our results, we give several examples of such operator matrices.

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